

## ASSIGNMENT 2 (COMPULSORY)

Due Date	Unique Number
23 March 2018	680827

Submit your answers online through myUnisa. No extensions will be granted for submission of this assignment. **NO** manual or posted submissions will be allowed.

Questions 1 and 2 are based on the information below:

An energy company in the West Coast District Municipality charges residential customers a basic fee of R150.00, and R0.50c per kilowatt hour (kWh).

### Question 1

Define the utility function  $y(x)$  for a household in this municipality. Let  $x$  represent the total number of kWh consumed per household.

- 1)  $y(x) = 150x + 0.5$
- 2)  $y(x) = 0.5x + 75$
- 3)  $y(x) = 75x + 0.5$
- 4)  $y(x) = 0.5x + 150$

### Question 2

If there are 700 000 households in this municipality, find the revenue function  $R(x)$ , in rands, for the municipality. Let  $x$  be the total kWh consumed by all households.

- 1)  $R(x) = 350\,000x + 105\,000\,000$
- 2)  $R(x) = 150\,000x + 700\,000$
- 3)  $R(x) = 0.5x + 105\,000\,000$
- 4)  $R(x) = 0.5x + 700\,000$

Questions 3 to 5 are based on the information below:

Andrea Publishers is a book publisher based in Johannesburg. The total cost (in rands) of producing  $x$  high school maths study guides is given by the function:

$$C(x) = 89.9x + 120\,000$$

### Question 3

What are the fixed costs for Andrea Publishers in producing the maths study guides?

- 1) R10 788.00
- 2) R1 334.82
- 3) R10 788 000.00
- 4) R120 000.00

### Question 4

What is the total cost of producing 1000 study guides?

- 1) R100 688.00
- 2) R209 900.00
- 3) R89 900.00
- 4) R9 324.82

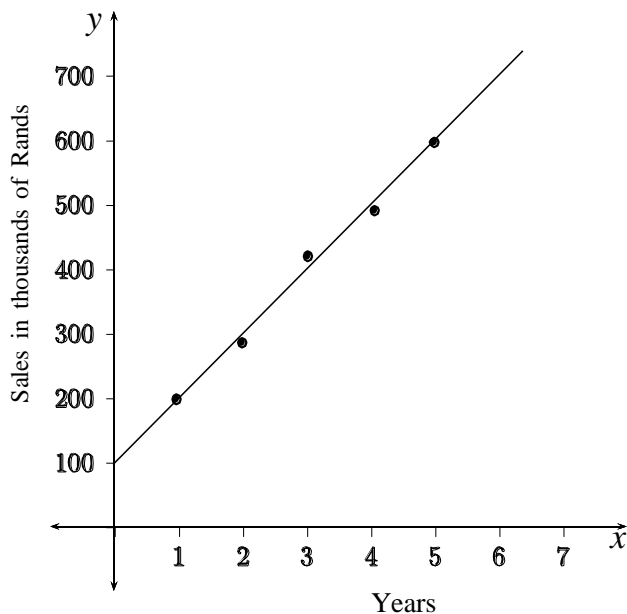
### Question 5

What is the average cost per book when producing 1000 books?

- 1) R89.90
- 2) R92.34
- 3) R209.90
- 4) R100.69

Questions 6 and 7 are based on the information below:

For the past five years, Thabo and Eric run a local iKota take-away restaurant in their township. They plotted the restaurant sales vs time since they started their operation. They found that the plotted points lie approximately along a straight line. This is shown by the figure below:



### **Question 6**

Using the points corresponding to the first and fifth year, find the equation of the sales trend line.

- 1)  $y = 200x + 100$
- 2)  $y = 2x + 100$
- 3)  $y = 100x + 100$
- 4)  $y = x + 100$

### **Questions 7**

Using the sales trend line, what sales figures can be expected for the sixth year?

- 1) R1 300 000
- 2) R700 000
- 3) R112 000
- 4) R106 000

*Question 8 and 9 are based on the following information:*

*The annual sales (in billions of rand) of notebooks from 2006 to 2012 are shown in the following table. ( $x=0$  corresponds to the year 2006)*

Year, $x$	0	1	2	3	4	5	6
Annual Sales	7.9	9.6	11.5	13.3	15.2	17	18.8

### **Question 8**

Derive the equation ( $L = y(x)$ ) of the line through the points corresponding to the years 2006 and 2012.

- 1)  $y = 1.82x + 7.9$
- 2)  $y = 1.96x + 7.9$
- 3)  $y = 1.85x + 7.9$
- 4)  $y = 1.84x + 7.9$

### **Question 9**

Use the equation of the line L to estimate annual sales of notebooks in the year 2011.

- 1) R15.2 billion
- 2) R17 billion
- 3) R18.8 billion
- 4) R7.9 billion

**Question 10**

Which of the following statement is incorrect about the parabola:  $y = ax^2 + bx + c$

- 1) If  $|a| > 1$ , the parabola appears narrow than the graph of  $y = x^2$
- 2) The parabola is symmetric about the x-axis.
- 3) The highest point of a downward opening parabola is called the vertex.
- 4) If  $a < 0$ , the parabola opens downwards.

*Questions 11 to 13 are based on the information below:*

*Consider the function:  $y(x) = 2(x - 3)^2 + 1$ , and its graph.*

**Question 11**

Which of the following points are NOT on the graph?

- 1) (7;33)
- 2) (3;1)
- 3) (0;19)
- 4) (1;5)

**Question 12**

Find the x-intercept of this graph.

- 1) There are no x-intercept.
- 2) (0; 1) and (0; 3)
- 3) (0; -1) and (0; 2)
- 4) (0; -3) and (0; 1)

**Question 13**

Find the vertex of the graph.

- 1) (-1; 3)
- 2) (3; 1)
- 3) (-1; 3)
- 4) (3; -1)

**Question 14**

The estimated monthly profit (in rands) realizable by the Masai Company for manufacturing and selling  $x$  units of the Shuka Cloth is:

$$P(x) = -0.04x^2 + 240x - 1000$$

In order to maximize profits, how many units should the company produce and sell?

- 1) 1000 units
- 2) 2000 units
- 3) 3000 units
- 4) 4000 units

*Questions 15 and 16 are based on the information below:*

*A travel agency charges R300 per person for a luxury train trip, if exactly 200 people sign up for the trip, then each fare is reduced by R1 of each additional person. Let  $x$  denote the number of passengers above 200.*

**Question 15**

Define the revenue function  $R(x)$  for the revenue for the travel agency, where  $R$  is given in rands.

- 1)  $R(x) = -x^2 + 60x + 100\,000$
- 2)  $R(x) = x^2 - 60x + 100\,000$
- 3)  $R(x) = -x^2 + 100x + 60\,000$
- 4)  $R(x) = x^2 - 60x + 60\,000$

**Question 16**

How many sign-ups will help the travel agency realize their maximum profit?

- 1) 300 sign-ups
- 2) 250 sign-ups
- 3) 200 sign-ups
- 4) 350 sign-ups

**Question 17**

Consider the graph of the function  $y = a^x$ , when  $x > 1$ . Which of the following statement is incorrect about the graph?

- 1) The  $y$ -intercept is 1.
- 2) The graph climbs steeply to the right.
- 3) The graph cuts the negative  $x$  - axis.
- 4) The larger the base,  $a$ , the more steeply the graph rises to the right.

**Question 18**

Consider the graph of the function  $y = a^x$ , when  $0 < a < 1$ . Which of the following statement is incorrect about the graph?

- 1) The graph climbs steeply to the right.
- 2) The  $y$  – *intercept* is 1.
- 3) The graph does not cut the positive  $x$  – *axis*.
- 4) The smaller the base,  $a$ , the more steeply the graph falls to the right.

**Question 19**

Solve the following system of equations:

$$\begin{aligned}3x - 2y &= 4 \\ -6x + 4y &= 7\end{aligned}$$

- 1)  $x = 2$  and  $y = 1$
- 2)  $x = -4$  and  $y = 3$
- 3)  $x = 1$  and  $y = -2$
- 4) *No solutions*

**Question 20**

A shop sells bicycles and tricycles. In total, there are 7 cycles (this includes both bicycles and tricycles) and 19 wheels. Determine how many of each there are, if a bicycle has two wheels and a tricycle has three wheels.

- 1) 4 tricycles and 3 bicycles.
- 2) 2 tricycles and 5 bicycles.
- 3) 5 tricycles and 2 bicycles.
- 4) 6 tricycles and 1 bicycles.

**Question 21**

A fruit juice costs R2.00 more than a milkshake. If 3 fruit juices and 5 milkshakes cost R78.00, determine the individual prices.

- 1) One milkshake is R9.00 and one fruit juice is R11.00.
- 2) One milkshake is R8.00 and one fruit juice is R10.00.
- 3) One milkshake is R12.00 and one fruit juice is R13.00.
- 4) One milkshake is R10.00 and one fruit juice is R12.00.

**Question 22**

George has 1 litre of a mixture containing 69% salt concentration. How much water must George add to make the mixture 50% salt concentration?

- 1) 690ml
- 2) 380ml
- 3) 500ml
- 4) 1000ml

**Question 23**

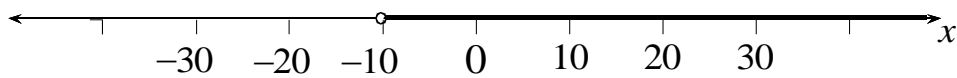
Which one of the following inequalities best describes the number line?



- 1)  $3 < x \leq 6$
- 2)  $3 \leq x \leq 6$
- 3)  $3 < x < 6$
- 4)  $3 \leq x < 6$

**Question 24**

Which of the following inequalities best describes the number line?



- 1)  $x \geq -10$
- 2)  $x > -10$
- 3)  $x \leq -10$
- 4)  $x < -10$

**Question 25**

A doctor advises a client who is suffering from iron and vitamin B deficiency to take at least 2400 milligrams (mg) of iron, 2100mg of vitamin B<sub>1</sub> and 1500mg of vitamin B<sub>2</sub> over a period of time. Two vitamin pills are suitable, brand A and brand B. Each brand A pill consists of 40mg of iron, 10mg of vitamin B<sub>1</sub> and 5mg of vitamin B<sub>2</sub>. Each of brand B pill consists of 10mg of iron, 15mg of vitamin B<sub>1</sub>, and 15mg of vitamin B<sub>2</sub>. Let  $x$  represent the number of brand A pills and  $y$  represent the number of brand B pills. Which one of the following systems of linear inequalities best represents the constraints given by this situation?

- 1)  $40x + 10y \geq 2400$ ;  $15x + 10y \geq 1500$ ;  $15x + 5y \geq 2100$ ;  $x \geq 0$ ;  $y \geq 0$ .
- 2)  $10x + 40y \geq 2100$ ;  $10x + 15y \geq 2400$ ;  $5x + 15y \geq 1500$ ;  $x \geq 0$ ;  $y \geq 0$ .
- 3)  $10x + 40y \geq 2400$ ;  $15x + 10y \geq 2100$ ;  $15x + 5y \geq 1500$ ;  $x \geq 0$ ;  $y \geq 0$ .
- 4)  $40x + 10y \geq 2400$ ;  $10x + 15y \geq 2100$ ;  $5x + 15y \geq 1500$ ;  $x \geq 0$ ;  $y \geq 0$ .