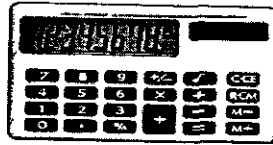


UNIVERSITY EXAMINATIONS



UNIVERSITEITSEKSAMENS  
**UNISA**   
university  
of south africa

**CSY3601**

January/February 2016

**CONTROL SYSTEMS III (THEORY)**

Duration 3 Hours

100 Marks

**EXAMINERS**

FIRST

SECOND

EXTERNAL

PROF G QI

PROF Z WANG

DR AA YUSUFF

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**Programmable pocket calculator is permissible**

**Partial/limited open book examination. Specified material as indicated on examination paper, permissible**

**This examination question paper remains the property of the University of South Africa and may not be removed from the examination venue**

This examination question paper consists of 6 pages including this "cover" page,

Partial Open book exam Ogata, K Modern Control Engineering

Answer all the questions

Please note: IF YOU ARE OF THE OPINION THAT INSUFFICIENT INFORMATION IS SUPPLIED FOR YOU TO ANSWER A PARTICULAR QUESTION, MAKE A REALISTIC ASSUMPTION, MOTIVATE IT AND THEN ANSWER THE QUESTION.

### QUESTION 1 MULTIPLE CHOICE QUESTIONS

- 1 1 In Bode diagrams, which of the following portion represents the high frequency noise resistant ability?
- A low frequency part      B median frequency part
- C high frequency part      D none
- 1 2 For the first and the second order systems, all coefficients of the system characteristic equation are all positive is the (      ) condition of system stability
- A sufficient condition      B necessary condition
- C sufficient and necessary condition      D none
- 1 3 The open loop transfer function of a system is  $G(s)H(s) = \frac{K}{s^3(s+4)}$ , then the root locus on the real axis is
- A  $[-4, \infty)$       B  $[-4, 0]$
- C  $(-\infty, -4]$       D  $[0, \infty)$
- 1 4 The maximum overshoot  $\sigma_p$  of a system represents which of the following performance?
- A. Relative stability      B. Absolute stability
- C. Responding speed      D. Steady state performance

- 15 If a second order system has damping ratio  $\zeta > 1$ , then the system characteristic roots are
- A two unequal negative real  
B two equal negative real  
C two equal positive real      D two unequal positive real
- 16 The open loop transfer function of a unit negative feedback system is  $G_o(s) = \frac{9}{s(s+6)}$ . The damping ratio is
- A  $\frac{1}{2}$       B. 1      C 2      D 4
- 17 The step function with magnitude  $x_0$  is
- A  $r(t) = 1(t)$       B  $r(t) = x_0$       C  $r(t) = x_0 \delta(t)$       D  $r(t) = x_0 \cdot 1(t)$

[14]

**QUESTION 2 CIRCUIT ANALYSIS, STEADY STATE ERROR**

Figure Q2 illustrates an RLC circuit. The capacitor has capacitance  $C$ , the inductor has inductance  $L$ , and the resistor resistance  $R$ . The input is the applied voltage  $v_i(t)$  and the output is the voltage across the capacitor  $v_o(t)$ .

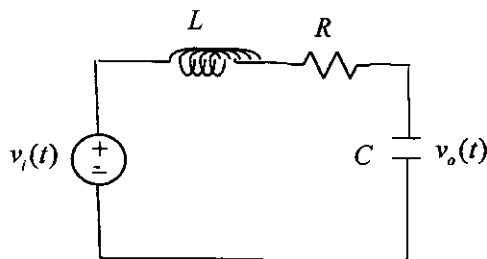


Figure Q2

- 2.1 Determine the transfer function relating  $v_o$  to  $v_i$  (5)
- 2.2 Let  $v_i(t)$  be a unit step applied at  $t = 0$ . Use the final value theorem to find the steady-state value of  $v_o(t)$  (5)
- 2.3 Set  $L = 0.5$  H and  $C = 4 \times 10^{-6}$  F. Derive the value of  $R$  so that the response is damping ratio is  $\zeta = 0.707$  (10)
- [20]**

### QUESTION 3 STEADY STATE ERRORS

A unity feedback system is shown in Figure Q3

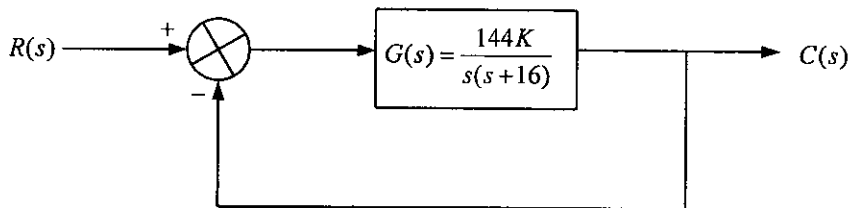


Figure Q3

- 3.1 For the transfer function  $G(s)$ , determine the type of system (4)
- 3.2 Find the error constants and steady-state errors for the basic types of inputs
- 3.2.1 2 step input, i.e.  $R(s) = \frac{2}{s}$ , (3)
- 3.2.2 Unit ramp input  $R(s) = \frac{1}{s^2}$  (3)
- [10]**

### QUESTION 4. STABILITY

The closed-loop system has the following characteristic equation. Using the Routh Criterion determine the number of roots of each equation that are in the right-half-plane and stability

$$s^3 + 25s^2 + 10s + 450 = 0$$

**[6]**

**QUESTION 5 ROOT LOCUS**

The unity negative feedback system has an open loop transfer function  $G(s)$  given by

$$G(s) = \frac{K(s+10)(s+5)}{(s-1)(s-5)}$$

- 5.1 Find the breakaway and break-in point manually (8)
- 5.2 Find the closed-loop transfer function and characteristic equation manually in terms of  $K$ . Using Routh-Hurwitz criterion find the value of  $K$  for which the closed-loop is marginally stable, i.e. the root-locus cross the imaginary axis manually. Find the cross frequency manually (12)
- 5.3 Use information obtained in Question 3.1 and 3.2 to sketch the locus of the closed-loop system and mark the position of breakaway, break-in points and imaginary axis crossing point (5)

**[25]****QUESTION 6 BODE DIAGRAMS**

Sketch straight line approximations for the magnitude and phase Bode plots for a system with an open-loop transfer function  $G(s)$  given by

$$G(s) = \frac{10(s+1)}{(s+5)(s+50)}$$

- 6.1 Give the frequency response form and magnitude response form  $G(j\omega)$  according to the open-loop transfer function, and determine the magnitude in dB (6)
- 6.2 Describe the approximate properties of Bode plots at low frequency and high frequency (10)
- 6.3 Sketch the Bode plots using the information obtained in Question 4.1 and 4.2 (9)

**[25]****[TOTAL: 100]**