

## CSY3601

January/February 2017

### CONTROL SYSTEMS III (THEORY)

Duration 3 Hours

100 Marks

**EXAMINERS**

FIRST

SECOND

EXTERNAL

PROF Z WANG

DR X YE

DR AA YUSUFF

---

**Programmable pocket calculator is permissible**

**Closed book examination**

**This examination question paper remains the property of the University of South Africa and may not be removed from the examination venue**

This examination question paper consists of 3 pages including this "cover" page,

Partial Open book exam Ogata, K Modern Control Engineering

Answer all the questions

**PLEASE NOTE: IF YOU HAVE THE OPINION THAT INSUFFICIENT INFORMATION IS SUPPLIED FOR YOU TO ANSWER A PARTICULAR QUESTION, MAKE A REALISTIC ASSUMPTION, MOTIVATE IT AND THEN ANSWER THE QUESTION.**

### QUESTION 1

Consider the circuit shown in Figure 1

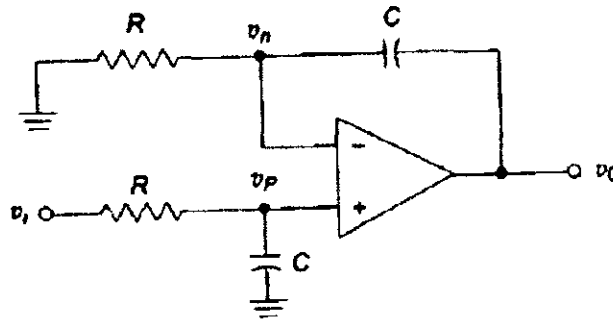


Figure 1: Circuit for Question 1

Find the transfer function  $H(s) = \frac{V_o(s)}{V_i(s)}$  of this system

[18]

### QUESTION 2

The dynamic equation of a second order system is given by

$$\frac{d^2 y(t)}{dt^2} + \frac{4dy(t)}{dt} + 16y(t) = 16x(t),$$

and all initials are zero

Determine:

- 2.1 Transfer function  $G(s) = \frac{Y(s)}{X(s)}$ , (5)
- 2.2 Damping factor  $\xi$ , (3)
- 2.3 Undamped natural frequency  $\omega_n$ , (3)
- 2.4 Damped natural frequency  $\omega_d$ , (3)
- 2.5 Delay time  $t_d$ , (3)
- 2.6 Rise time  $t_r$ , (3)
- 2.7 Peak time  $t_p$ ; (3)

[TURN OVER]

- 2.8 Maximum overshoot  $M_p$ , (3)
- 2.9 Settling time  $t_s$  (5% criterion) (3)
- [29]

**QUESTION 3**

The open-loop transfer function  $G(s)$  of a unity negative feedback system is given by

$$G(s) = \frac{K}{s(s+2)(s+4)}$$

- 3.1 Calculate the break-away points (8)
- 3.2 Determine the  $j\omega$ -axis crossings and the gain,  $K$ , at the  $j\omega$ -axis crossing based on the Routh's stability criterion (13)
- 3.3 Sketch the root locus (12)
- [33]

**QUESTION 4**

The open loop transfer function of a unity feedback system is given by

$$G(s) = \frac{2 \times 10^3 s(s+2)}{(s+1)(s+20)}$$

Sketch the Bode diagrams of the system using the asymptotic method.

Hint the procedure is necessary

[20]

**TOTAL: 100**