



# DIG1501

May/June 2017

## DIGITAL SYSTEMS I (THEORY)

Duration 3 Hours

100 Marks

**EXAMINERS**

FIRST

SECOND

MR PO UMENNE

MR NR NETSHIKWETA

**Programmable pocket calculator is permissible**

**Closed book examination**

**This examination question paper remains the property of the University of South Africa and may not be removed from the examination venue**

This examination question paper consists of 6 pages including the cover page and a formula sheet

Answer all the questions

**PLEASE NOTE; IF YOU HAVE THE OPINION THAT INSUFFICIENT INFORMATION IS SUPPLIED FOR YOU TO ANSWER A PARTICULAR QUESTION, MAKE A REALISTIC ASSUMPTION, MOTIVATE IT AND THEN ANSWER THE QUESTION.**

### NUMBER SYSTEMS, OPERATION AND CODES

#### QUESTION 1

1 1 In the 2's complement form, the binary number 10010011 is equal to which decimal number

(4)

1 2 Determine the decimal value of the following signed binary number in the 2's complement form

10011001

(4)

**[8]**

#### QUESTION 2

The binary number 10001101010001101111 can be written in hexadecimal as \_\_\_\_\_

(3)

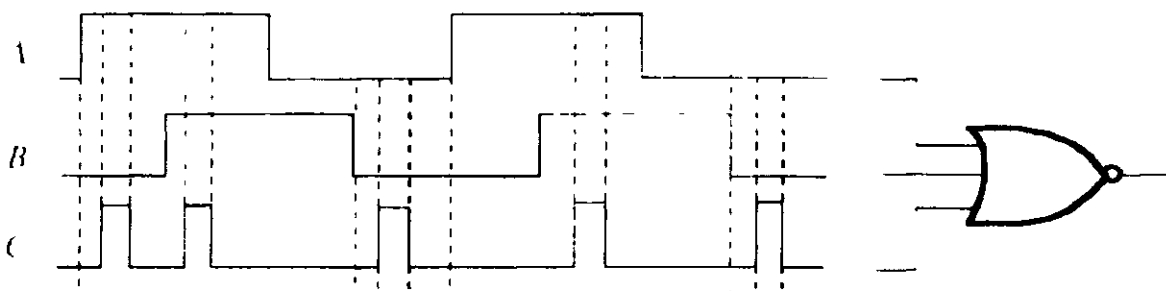
**[3]**

### LOGIC GATES

#### QUESTION 3

Determine the output waveform in figure 1 below and draw the timing diagram. (5)

**[5]**



**Figure 1**

TURN OVER

## QUESTION 4

For the set of input waveforms in figure 2, determine the output for the gate shown and draw the timing diagram (5)

[5]

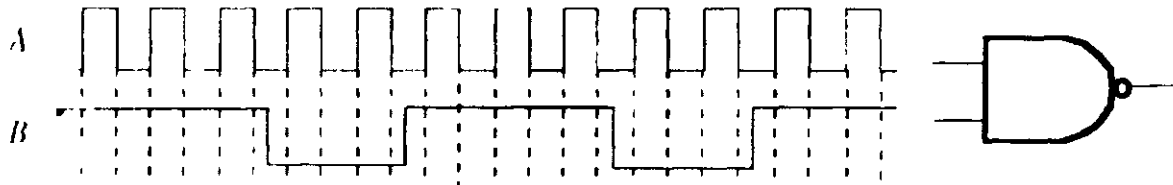


Figure 2

## BOOLEAN ALGEBRA AND LOGIC SIMPLIFICATION

## QUESTION 5

5 1 Apply De Morgan's theorem to the expression below

$$\overline{(CD + \bar{E}F)(\bar{A}B + \bar{C}D)} \quad (6)$$

5 2 Using Boolean algebra simplify the following expression

$$(B + BC)(B + \bar{B}C)(B + D) \quad (6)$$

5 3 Use a Karnaugh map to find the minimum SOP form for the following expression

$$\bar{A}(BC + B\bar{C}) + A(BC + B\bar{C}) \quad (8)$$

5 4 Use a Karnaugh map to reduce the following expression to a minimum SOP form

$$\bar{A}B(\bar{C}\bar{D} + \bar{C}D) + AB(\bar{C}\bar{D} + \bar{C}D) + A\bar{B}\bar{C}D \quad (10)$$

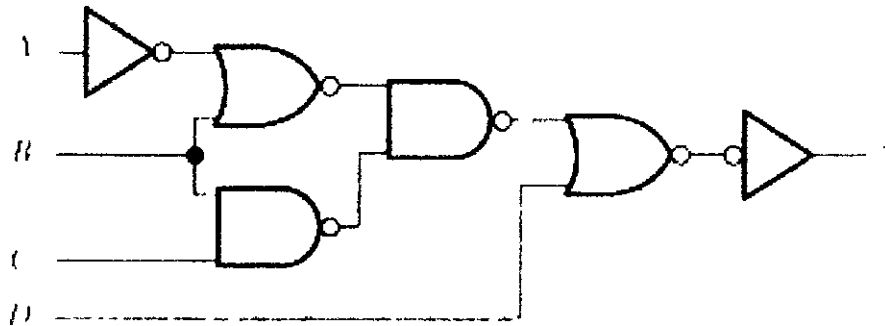
[30]

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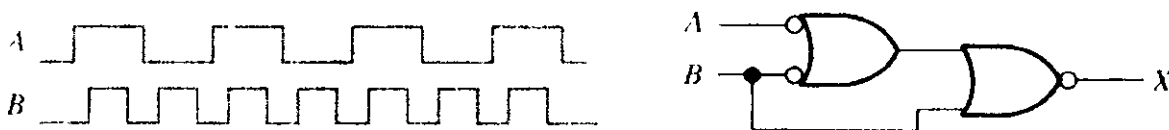
**COMBINATIONAL LOGIC ANALYSIS****QUESTION 6**

6.1 Develop the truth table for the circuit in figure 3 below

(16)

**Figure 3**

6.2 Given the logic circuit and the input waveforms in figure 4 below, sketch the output waveform (6)

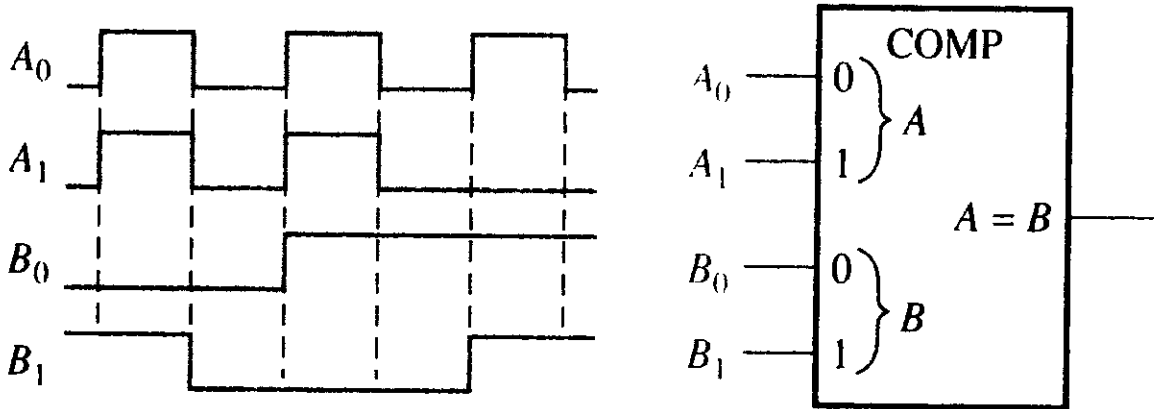
**Figure 4****[22]**

TURN OVER

**FUNCTIONS OF COMBINATIONAL LOGIC**

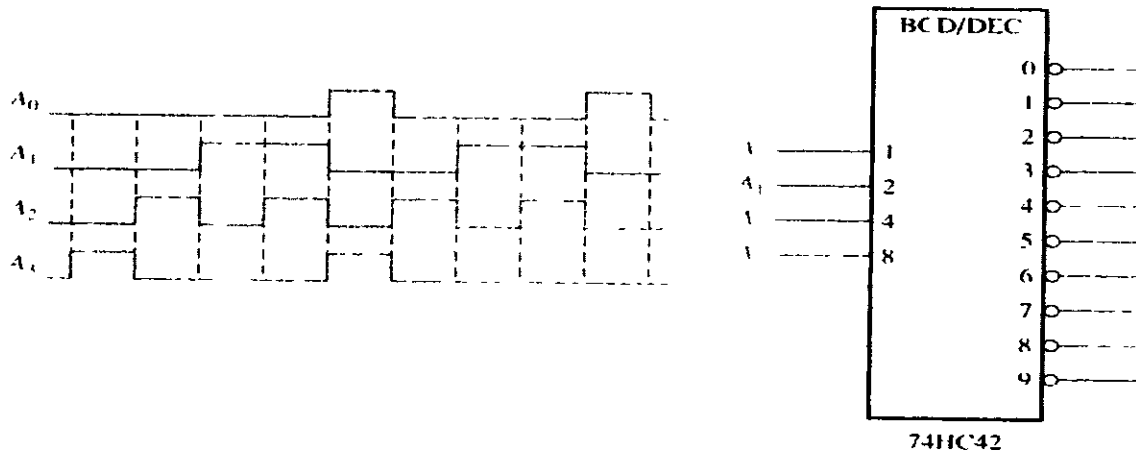
**QUESTION 7**

7.1 The waveforms in figure 5 below are applied to the comparator as shown. Determine the output ( $A = B$ ) waveform (6)



**Figure 5**

7.2 BCD (Binary coded decimal) numbers are applied sequentially to the BCD-to-decimal decoder in figure 6 below. Draw a timing diagram, showing each output in the proper relationship with the others and with the inputs. (Hint  $A_3$  is the most significant bit). (10)



**Figure 6**

TURN OVER

- 7.3 For the parallel adder in figure 7 below determine the complete sum by analysis of the logical operation of the circuit. Verify your result by long hand addition of the two input numbers. (11)

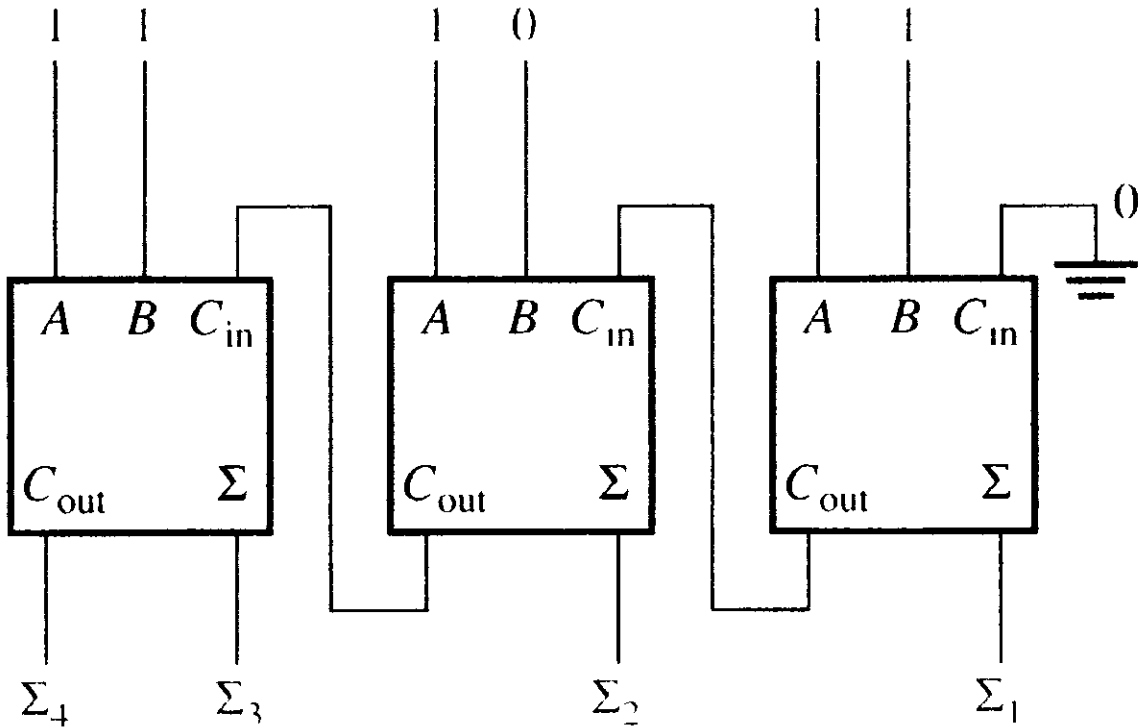


Figure 7

[27]

Total Marks [100]

DIG1501

**DIGITAL SYSTEMS I  
FORMULAE SHEET**

**Basic Laws**

$$X \cdot 0 = 0$$

$$X + 0 = X$$

$$X \cdot 1 = X$$

$$X + 1 = 1$$

$$X \cdot X = X$$

$$X + X = X$$

$$X \cdot \bar{X} = 0$$

$$X + \bar{X} = 1$$

$$\overline{\bar{X}} = X$$

**Commutative Laws**

$$X \cdot Y = Y \cdot X$$

$$X + Y = Y + X$$

**Associative Laws**

$$(X + Y) + Z = X + (Y + Z) = X + Y + Z$$

$$(X \cdot Y) \cdot Z = X \cdot (Y \cdot Z) = X \cdot Y \cdot Z$$

**Distributive Laws**

$$X \cdot (Y + Z) = (X \cdot Y) + (X \cdot Z)$$

$$X + (Y \cdot Z) = (X + Y) \cdot (X + Z)$$

**De Morgan's Theorem**

$$\overline{X \cdot Y} = \bar{X} + \bar{Y}$$

$$X + \bar{Y} = \overline{X \cdot \bar{Y}}$$

**Logic Theorems**

$$X + X \cdot Y = X \text{ (Absorption)}$$

$$X + \bar{X} \cdot Y = X + Y$$

$$X \cdot Y + Y \cdot \bar{Y} = X \text{ (logical identity)}$$

$$X \cdot Z + \bar{X} \cdot Y \cdot Z = X \cdot Z + Y \cdot Z$$

$$X \cdot Y + X \cdot Z + \bar{Y} \cdot Z = X \cdot Y + \bar{Y} \cdot Z$$