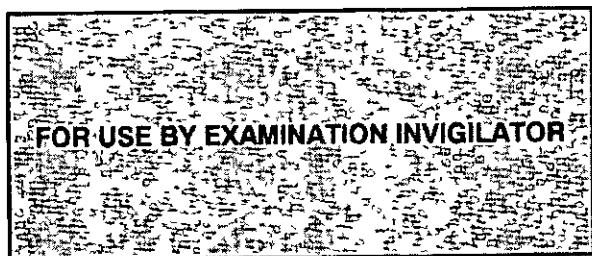




ECS3706

OCTOBER / NOVEMBER 2017

## ECONOMETRICS



**Subject**

### **Number of paper**

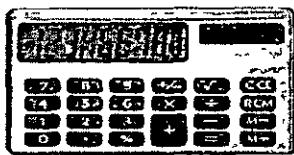
**Date of examination**

## Examination centre

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ECS3706

October/November 2017

# ECONOMETRICS

EXAMINERS

FIRST MR MJ KHUMALO  
SECOND PROF TLA LESHORO  
EXTERNAL DR LJ RAPUTSOANE

**Use of a non-programmable pocket calculator is permissible**

### **Closed book examination**

This examination question paper remains the property of the University of South Africa and may not be removed from the examination venue

This paper consists of 32 pages, including a formulae sheet (p24), 3 pages of statistical tables (pp 25 to 27), 5 pages for rough work (pp 28 to 32) plus the special front page

This paper consists of two sections

**Section A:** Answer all 4 questions which together count 60 marks ( $15 + 15 + 15 + 15$ ) = 60  
**Section B:** Answer any 2 of the 3 questions Each question counts 20 marks ( $2 \times 20$ ) = 40  
Total = 100

**SECTION A (60 marks)**

**Answer ALL four questions in section A**

Section A requires brief and to the point answers

In most cases simply list, or briefly explain what is required

It may be advantageous to use statistical notation (mathematical symbols) to explain concepts, but make sure to also explain their meaning.

It is not required to re-explain concepts that have been previously dealt with. If required, you may simply refer to your previous answer/s.

In general, each mark represents one correct fact or correct interpretation

You have 120 minutes to earn 100 marks in the case of the complete paper, that is, 6 minutes per 5 marks.

**SECTION A (60 marks)**

Answer **ALL** four questions in section A

**QUESTION 1 (15 marks)**

- (a) Briefly explain two weaknesses or shortcomings of econometrics (3)

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- (b) In evaluating regression estimates do you consider statistical tests to be more important than economic theory? In your answer also briefly explain why economic theory is important in econometrics (6)

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- (c) Briefly explain what OLS means, what the OLS method tries to achieve and the principles on which the OLS method is based. Also list any three good characteristics of OLS (6)

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[15]

**QUESTION 2 (15 marks)**

A researcher obtained the following ordinary least squares (OLS) regression results on the linear relationship between consumption  $Y_i$  (measured in rands per month) and income  $X_i$  (measured in rands)

$$\bar{X} = 60.5, \bar{Y} = 55.251, \sum_{i=1}^N X_i = 6050, \sum_{i=1}^N Y_i = 5525.11, \sum_{i=1}^N Y_i^2 = 232868, \sum_{i=1}^N X_i^2 = 760629 \\ , \sum_{i=1}^N X_i Y_i = 389755, \sum_{i=1}^N x_i y_i = 2490, \sum_{i=1}^N y_i^2 = 1872.25, \sum_{i=1}^N x_i^2 = 3830, \sum_{i=1}^N e_i^2 = 7489$$

- (a) Using the sample information and assuming that the regression equation is of the form  $Y_i = \beta_0 + \beta_1 X_i + \varepsilon_i$ , calculate the OLS estimates of the intercept  $\hat{\beta}_0$  and the slope coefficient  $\hat{\beta}_1$ ,  $R^2$  and the explained sum of squares (ESS) (show calculations). What is the sample size of this regression? (13)

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[TURN OVER]

- (b) What is the meaning of  $\sum_{i=1}^N e_i^2 = 7489$  provided above? (2)

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[15]

**[TURN OVER]**

**QUESTION 3 (15 marks)**

A two variable regression has the following results

Source of variation	Sum of squares (SS)	Degrees of freedom (d.f.)	MSS = SS/d.f.
Due to regression(ESS)	66965	-	-
Due to residual (RSS)	-	-	-
Total (TSS)	67052	29	-

- (a) What is the sample size (N)? (2)

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- (b) What is the value of RSS? (2)

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- (c) What are the degrees of freedom (d.f.) of the ESS and RSS? (4)

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- (d) What are the values of  $R^2$  and adjusted  $R^2$ ? Interpret the  $R^2$  obtained (3)

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(e) What is the value of the F-statistic? (4)

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**[15]**

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**QUESTION 4 (15 marks)**

Discuss the problem of serial correlation

- (a) Briefly explain its nature the meaning of pure and impure serial correlation Also explain what the meaning of first-order serial correlation is (5)

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- (b) List the consequences of pure serial correlation (3)

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**[TURN OVER]**

- (c) Explain how serial correlation may be detected by the use of the DW-d statistic (4)

- (d) Explain a situation in which heteroscedasticity can be remedied by redefining the variables (3)

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**[15]****SUBTOTAL SECTION A [60]****[TURN OVER]**

**SECTION B (40 marks)**

**Answer ANY TWO of the THREE QUESTIONS** in section B      Each question counts 20 marks

- Section B mostly consists of practical problems
  - Use a 5% level of significance in statistical testing, unless stated otherwise

**QUESTION B1 (20 marks)**

A researcher estimated the demand for rice model and found the following results. The Dependent variable: Rice

Variable	Coefficient	t-statistic	Other Statistics
Constant	4 2854	8 104	R <sup>2</sup> = 0 56
P <sub>r</sub>	-0 0094	1 907	Durbin-Watson = 1 5736
Y	0 03917	0 841	F-statistic = 71 96
P <sub>PS</sub>	4 5529	10 475	
P <sub>MM</sub>	-0 2456	1 387	

Where  $P_B$  = price of energy drink

**Y** = Income of consumer

$P_{SP}$  = Price of substitute product

**P<sub>MM</sub>** = Price of maize meal

stic at 5% is 2.253

### Official Stations at 5% to 25%

- (a) Evaluate these results with respect to its economic meaning, overall fit, signs and significance of coefficients (16)

[TURN OVER]

[TURN OVER]

- (b) What econometric problem(s) (if any) does this regression have? How would you solve the problem(s) associated with this model? (4)

[TURN OVER]

10/11 2017

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**QUESTION B2 (20 marks)**

Suppose the original regression on demand for cars is given as follows. The dependent variable is represented by Y

Variable	constant	$\log X_1$	$\log X_2$	$\log X_3$	$\log X_4$
Coefficients	11.05	1.8504	-4.6792	2.6462	-0.0395
t-statistic	(0.652)	(1.408)	(-2.701)	(1.6129)	(-0.1268)

Adjusted  $R^2 = 0.7662$ , correlation coefficient between  $X_1$  and  $X_2$  ( $X_{1,2}$ ) = 0.995

The critical t-statistic at 5% level of significance is 1.67

Log Y = quantity demanded for passenger cars

Log X1 = price of new car

Log X2 = inflation

Log X3 = income

Log X4 = interest rate

[TURN OVER]

Two other regressions were done, first dropping  $X_2$  and secondly, dropping  $X_1$  and comparing the two regressions with the original regression. The regressions for the two equations are

	Variable	constant	LogX <sub>1</sub>	LogX <sub>2</sub>	LogX <sub>3</sub>	LogX <sub>4</sub>	Adjusted R <sup>2</sup>
Regression 1	Coefficient (t-statistic)	-22.05 (-0.652)	-1.051 (-3.408)		-0.592 (-5.613)	3.195 (3.718)	Adj-R <sup>2</sup> = 0.689
Regression 2	Coefficient (t-statistic)	-27.557 (-3.678)		-0.409 (-4.194)	-0.152 (-4.407)	3.296 (5.562)	Adj-R <sup>2</sup> = 0.787

- (a) Which regression between the original, regression 1 and regression 2 would you prefer and why? (10)

[TURN OVER]

[TURN OVER]

- (b) If the same variables are regressed in their original forms, that is, using a linear OLS without logs, how would you interpret the estimation results from the original equation if the coefficients were the same? (10)

[TURN OVER]

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[TURN OVER]

**QUESTION B3 (20 marks)**

A regression has been run to estimate the average hourly wages of full time workers. For the purpose of this let

AHE = average hourly earnings (constant 1998=100)

University = binary variable (1 if in university, 0 if in high school)

Female = binary variable (1 if female, 0 if male)

Age = age in years

North, East, South = binary variables (1 if in region, 0 otherwise)

$$\text{AHE} = 3.75 + 5.44 (\text{University}) - 2.62 (\text{Female}) + 0.29 (\text{Age}) + 0.69 (\text{North}) + 0.60 (\text{East}) - 0.27 (\text{South})$$

Other statistics  $R^2 = 0.194$ ,  $n = 4000$

- (a) Do there appear to be important regional differences (3)

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- (b) Why is the explanatory variable for region = West, omitted from the regression? What would happen if it was included? (3)

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[TURN OVER]

- (c) Joanne is a 26 year old female university graduate from the South region. Alejandro is a 35 year old male from the North who never attended any post school studies. Calculate the expected difference in earnings between Joanne and Alejandro. (7)

(d) An economist has derived the following macroeconomic production function  
 $\text{Log}(Q) = -1.60 + 0.41 \text{log}(K) + 0.62\text{log}(L) + 0.32\text{log}(T)$

Where

**Q** = production, **K** = capital input, **L** = technology and **T** = technology input

Briefly discuss this functional form, that is, explain its characteristics, and explain the major advantage of this form as well as the exact meaning of its slope coefficients.

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**[20]****[TURN OVER]**

**Appendix 1: Formulae sheet**

OLS estimates of  $Y_i = \beta_0 + \beta_1 X_{1i} + \varepsilon_i$

$$\hat{\beta}_1 = \frac{\sum x_{1i} y_i}{\sum x_{1i}^2} \text{ where } \begin{cases} x_{1i} = X_{1i} - \bar{X}_1 \\ y_i = Y_i - \bar{Y} \end{cases}$$

and  $i=1 \text{ to } n$

$$SE(\hat{\beta}_1) = \sqrt{\frac{\left( \sum e_i^2 \right)}{n-2}} \quad \sum x_{1i}^2$$

$$\hat{\beta}_0 = \bar{Y} - \hat{\beta}_1 \bar{X}_1 \text{ where } \bar{Y} = \sum_i Y_i / n \text{ and } \bar{X}_1 = \sum_i X_{1i} / n$$

TSS (Total sum of squares) = ESS (explained) + RSS (residual)

$$\sum y_i^2 = \sum (\hat{Y}_i - \bar{Y})^2 + \sum e_i^2$$

OLS estimates of  $Y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + \varepsilon_i$

$$\hat{\beta}_1 = \frac{\left( \sum y_i x_{1i} \right) \left( \sum x_{2i}^2 \right) - \left( \sum y_i x_{2i} \right) \left( \sum x_{1i} x_{2i} \right)}{\left( \sum x_{1i}^2 \right) \left( \sum x_{2i}^2 \right) - \left( \sum x_{1i} x_{2i} \right)^2} \quad \text{where } x_{2i} = X_{2i} - \bar{X}_2$$

$$\hat{\beta}_0 = \bar{Y} - \hat{\beta}_1 \bar{X}_1 - \hat{\beta}_2 \bar{X}_2$$

$$SE(\hat{\beta}_1) = \sqrt{\frac{\sum e_i^2 / (n-3)}{\sum x_{1i}^2 (1 - r_{x_1 x_2}^2)}}$$

$$r_{x_1 x_2} = \frac{\sum (X_{1i} - \bar{X}_1)(X_{2i} - \bar{X}_2)}{\sqrt{\sum (X_{1i} - \bar{X}_1)^2 (X_{2i} - \bar{X}_2)^2}}$$

Some statistical measures

$$t = \frac{\hat{\beta} - \beta_{H_0}}{SE(\hat{\beta})}$$

$$DW d = \frac{\sum_{i=2}^T (e_i - e_{i-1})^2}{\sum_{i=1}^T e_i^2}$$

$$F = \frac{ESS / K}{RSS / (n - K - 1)}$$

Table	Contents
1	Critical values of the t-distribution
2	Critical values of the F-distribution 5% level of significance
3	Critical values of the Durbin-Watson test statistic (DW-d) of $D_L$ and $D_U$ DW-d 5% one-sided and 10% two-sided level of significance

**Table 1 Critical values of the t-distribution**

Degrees of freedom	Level of significance					
	One-sided	10%	5%	2.5%	1%	0.5%
Two-sided	20%	10%	5%	2%	1%	
1	3 078	6 314	12 706	31 821	63 657	
2	1 886	2 920	4 303	6 965	9 925	
3	1 638	2 353	3 182	4 541	5 841	
4	1 533	2 132	2 776	3 747	4 604	
5	1 476	2 015	2 571	3 365	4 032	
6	1 440	1 943	2 447	3 143	3 707	
7	1 415	1 895	2 365	2 998	3 499	
8	1 397	1 860	2 306	2 896	3 355	
9	1 383	1 833	2 262	2 821	3 250	
10	1 372	1 812	2 228	2 764	3 169	
11	1 363	1 796	2 201	2 718	3 106	
12	1 356	1 782	2 179	2 681	3 055	
13	1 350	1 771	2 160	2 650	3 012	
14	1 345	1 761	2 145	2 624	2 977	
15	1 341	1 753	2 131	2 602	2 947	
16	1 337	1 746	2 120	2 583	2 921	
17	1 333	1 740	2 110	2 567	2 898	
18	1 330	1 734	2 101	2 552	2 878	
19	1 328	1 729	2 093	2 539	2 861	
20	1 325	1 725	2 086	2 528	2 845	
21	1 323	1 721	2 080	2 518	2 831	
22	1 321	1 717	2 074	2 508	2 819	
23	1 319	1 714	2 069	2 500	2 807	
24	1 318	1 711	2 064	2 492	2 797	
25	1 316	1 708	2 060	2 485	2 787	
26	1 315	1 706	2 056	2 479	2 779	
27	1 314	1 703	2 052	2 473	2 771	
28	1 313	1 701	2 048	2 467	2 763	
29	1 311	1 699	2 045	2 462	2 756	
30	1 310	1 697	2 042	2 457	2 750	
40	1 303	1 684	2 021	2 423	2 704	
50	1 299	1 676	2 009	2 403	2 678	
60	1 296	1 671	2 000	2 390	2 660	
70	1 294	1 667	1 994	2 381	2 648	
120	1 289	1 658	1 980	2 358	2 617	
Normal	1 282	1 645	1 960	2 326	2 576	

**[TURN OVER]**

Table 2: Critical values of the F-distribution 5% level of significance

		Degrees of freedom for numerator ( $v_1$ )											
		1	2	3	4	5	6	7	8	10	12	20	$\infty$
Degrees of freedom of denominator ( $v_2$ )	1	161.0	200.0	216.0	225.0	230.0	234.0	237.0	239.0	242.0	244.0	248.0	254.3
	2	18.5	19.0	19.2	19.2	19.3	19.3	19.4	19.4	19.4	19.4	19.4	19.5
	3	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.79	8.74	8.66	8.53
	4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	5.96	5.91	5.80	5.63
	5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.74	4.68	4.56	4.36
	6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.06	4.00	3.87	3.67
	7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.64	3.57	3.44	3.23
	8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.35	3.28	3.15	2.93
	9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.14	3.07	2.94	2.71
	10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	2.98	2.91	2.77	2.54
	11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.85	2.79	2.65	2.40
	12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.75	2.69	2.54	2.30
	13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.67	2.60	2.46	2.21
	14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.60	2.53	2.39	2.13
	15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.54	2.48	2.33	2.07
	16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.49	2.42	2.28	2.01
	17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.45	2.38	2.23	1.96
	18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.41	2.34	2.19	1.92
	19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.38	2.31	2.16	1.88
	20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.35	2.28	2.12	1.84
	21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.32	2.25	2.10	1.81
	22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.30	2.23	2.07	1.78
	23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.27	2.20	2.05	1.76
	24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.25	2.18	2.03	1.73
	25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.24	2.16	2.01	1.71
	26	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.22	2.15	1.99	1.69
	27	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.20	2.13	1.97	1.68
	28	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.19	2.12	1.96	1.66
	29	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.18	2.10	1.94	1.64
	30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.16	2.09	1.93	1.62
	40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.08	2.00	1.84	1.51
	50	4.03	3.18	2.79	2.56	2.40	2.29	2.20	2.13	2.03	1.95	1.78	1.44
	60	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	1.99	1.92	1.75	1.39
	70	3.98	3.13	2.74	2.50	2.35	2.23	2.14	2.07	1.97	1.89	1.72	1.36
	120	3.92	3.07	2.68	2.45	2.29	2.18	2.09	2.02	1.91	1.83	1.66	1.25
	$\infty$	3.84	3.00	2.60	2.37	2.21	2.10	2.01	1.94	1.83	1.75	1.57	1.00

[TURN OVER]

**Table 3 Critical values of the Durbin-Watson test statistics  $D_L$  and  $D_U$**   
**5% one-sided and 10% two-sided level of significance**

n	k'=1		k'=2		k'=3		k'=4		k'=5		k'=6		k'=7	
	$d_L$	$d_U$												
15	1.08	1.36	0.95	1.54	0.81	1.75	0.69	1.97	0.56	2.21	0.45	2.47	0.34	2.73
16	1.11	1.37	0.98	1.54	0.86	1.73	0.73	1.93	0.62	2.15	0.50	2.39	0.40	2.62
17	1.13	1.38	1.02	1.54	0.90	1.71	0.78	1.90	0.66	2.10	0.55	2.32	0.45	2.54
18	1.16	1.39	1.05	1.53	0.93	1.69	0.82	1.87	0.71	2.06	0.60	2.26	0.50	2.46
19	1.18	1.40	1.07	1.53	0.97	1.68	0.86	1.85	0.75	2.02	0.65	2.21	0.55	2.40
20	1.20	1.41	1.10	1.54	1.00	1.68	0.89	1.83	0.79	1.99	0.69	2.16	0.60	2.34
21	1.22	1.42	1.13	1.54	1.03	1.67	0.98	1.81	0.83	1.96	0.73	2.12	0.64	2.29
22	1.24	1.43	1.15	1.54	1.05	1.66	0.96	1.80	0.86	1.94	0.77	2.09	0.68	2.25
23	1.26	1.44	1.17	1.54	1.08	1.66	0.99	1.79	0.90	1.92	0.80	2.06	0.72	2.21
24	1.27	1.45	1.19	1.55	1.10	1.66	1.01	1.78	0.93	1.90	0.84	2.04	0.75	2.17
25	1.29	1.45	1.21	1.55	1.12	1.66	1.04	1.77	0.95	1.89	0.87	2.01	0.78	2.14
26	1.30	1.46	1.22	1.55	1.14	1.65	1.06	1.76	0.98	1.88	0.90	1.99	0.82	2.12
27	1.32	1.47	1.24	1.56	1.16	1.65	1.08	1.76	1.00	1.86	0.93	1.97	0.85	2.09
28	1.33	1.48	1.26	1.56	1.18	1.65	1.10	1.75	1.03	1.85	0.95	1.96	0.87	2.07
29	1.34	1.48	1.27	1.56	1.20	1.65	1.12	1.74	1.05	1.84	0.98	1.94	0.90	2.05
30	1.35	1.49	1.28	1.57	1.21	1.65	1.14	1.74	1.07	1.83	1.00	1.93	0.93	2.03
31	1.36	1.50	1.30	1.57	1.23	1.65	1.16	1.74	1.09	1.83	1.02	1.92	0.95	2.02
32	1.37	1.50	1.31	1.57	1.24	1.65	1.18	1.73	1.11	1.82	1.04	1.91	0.97	2.00
33	1.38	1.51	1.32	1.58	1.26	1.65	1.19	1.73	1.13	1.81	1.06	1.90	0.99	1.99
34	1.39	1.51	1.33	1.58	1.27	1.65	1.21	1.73	1.14	1.81	1.08	1.89	1.02	1.98
35	1.40	1.52	1.34	1.58	1.28	1.65	1.22	1.73	1.16	1.80	1.10	1.88	1.03	1.97
36	1.41	1.52	1.35	1.59	1.30	1.65	1.24	1.73	1.18	1.80	1.11	1.88	1.05	1.96
37	1.42	1.53	1.36	1.59	1.31	1.66	1.25	1.72	1.19	1.80	1.13	1.87	1.07	1.95
38	1.43	1.54	1.37	1.59	1.32	1.66	1.26	1.72	1.20	1.79	1.15	1.86	1.09	1.94
39	1.43	1.54	1.38	1.60	1.33	1.66	1.27	1.72	1.22	1.79	1.16	1.86	1.10	1.93
40	1.44	1.54	1.39	1.60	1.34	1.66	1.29	1.72	1.23	1.79	1.18	1.85	1.12	1.93
45	1.48	1.57	1.43	1.62	1.38	1.67	1.34	1.72	1.29	1.78	1.24	1.84	1.19	1.90
50	1.50	1.59	1.46	1.63	1.42	1.67	1.38	1.72	1.34	1.77	1.29	1.82	1.25	1.88
55	1.53	1.60	1.49	1.64	1.45	1.68	1.41	1.72	1.37	1.77	1.33	1.81	1.29	1.86
60	1.55	1.62	1.51	1.65	1.48	1.69	1.44	1.73	1.41	1.77	1.37	1.81	1.34	1.85
65	1.57	1.63	1.54	1.66	1.50	1.70	1.47	1.73	1.44	1.77	1.40	1.81	1.37	1.84
70	1.58	1.64	1.55	1.67	1.53	1.70	1.49	1.74	1.46	1.77	1.43	1.80	1.40	1.84
75	1.60	1.65	1.57	1.68	1.54	1.71	1.52	1.74	1.49	1.77	1.46	1.80	1.43	1.83
80	1.61	1.66	1.59	1.69	1.56	1.72	1.53	1.74	1.51	1.77	1.48	1.80	1.45	1.83
85	1.62	1.67	1.60	1.70	1.58	1.72	1.55	1.75	1.53	1.77	1.50	1.80	1.47	1.83
90	1.63	1.68	1.61	1.70	1.59	1.73	1.57	1.75	1.54	1.78	1.52	1.80	1.49	1.83
95	1.64	1.69	1.62	1.71	1.60	1.73	1.58	1.75	1.56	1.78	1.54	1.80	1.51	1.83
100	1.65	1.69	1.63	1.72	1.61	1.74	1.59	1.76	1.57	1.78	1.55	1.80	1.53	1.83

n=number of observations

k'=number of explanatory variables excluding the constant term

[TURN OVER]

**ROUGH WORK WILL NOT BE MARKED**

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