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ECS3706

OCTOBER / NOVEMBER 2017

ECONOMETRICS

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**ECS3706**

October/November 2017

ECONOMETRICS

Duration 2 Hours

100 Marks

EXAMINERS
 FIRST
 SECOND
 EXTERNAL

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 PROF TLA LESHORO
 DR LJ RAPUTSOANE

Use of a non-programmable pocket calculator is permissible

Closed book examination

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This paper consists of 32 pages, including a formulae sheet (p24), 3 pages of statistical tables (pp 25 to 27), 5 pages for rough work (pp 28 to 32) plus the special front page

This paper consists of two sections

Section A: Answer all 4 questions which together count 60 marks $(15 + 15 + 15 + 15) = 60$
Section B: Answer any 2 of the 3 questions Each question counts 20 marks $(2 \times 20) = 40$
 Total = 100

SECTION A (60 marks)

Answer **ALL** four questions in section A

Section A requires brief and to the point answers

In most cases simply list, or briefly explain what is required

It may be advantageous to use statistical notation (mathematical symbols) to explain concepts, but make sure to also explain their meaning

It is not required to re-explain concepts that have been previously dealt with. If required, you may simply refer to your previous answer/s

In general, each mark represents one correct fact or correct interpretation

You have 120 minutes to earn 100 marks in the case of the complete paper, that is, 6 minutes per 5 marks

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SECTION A (60 marks)

Answer **ALL** four questions in section A

QUESTION 1 (15 marks)

(a) Briefly explain two weaknesses or shortcomings of econometrics (3)

(b) In evaluating regression estimates do you consider statistical tests to be more important than economic theory? In your answer also briefly explain why economic theory is important in econometrics (6)

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[15]

QUESTION 2 (15 marks)

A researcher obtained the following ordinary least squares (OLS) regression results on the linear relationship between consumption Y_i (measured in rands per month) and income X_i (measured in rands)

$$\bar{X} = 60.5, \bar{Y} = 55\,251, \sum_{i=1}^N X_i = 6050, \sum_{i=1}^N Y_i = 5525\,11, \sum_{i=1}^N Y_i^2 = 232868, \sum_{i=1}^N X_i^2 = 760629$$

$$, \sum_{i=1}^N X_i Y_i = 389755, \sum_{i=1}^N x_i y_i = 2490, \sum_{i=1}^N y_i^2 = 1872\,25, \sum_{i=1}^N x_i^2 = 3830, \sum_{i=1}^N e_i^2 = 7489$$

- (a) Using the sample information and assuming that the regression equation is of the form $Y_i = \beta_0 + \beta_1 X_i + \varepsilon_i$, calculate the OLS estimates of the intercept $\hat{\beta}_0$ and the slope coefficient $\hat{\beta}_1$, R^2 and the explained sum of squares (ESS) (show calculations) What is the sample size of this regression? (13)

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(b) What is the meaning of $\sum_{i=1}^N e_i^2 = 7489$ provided above?

(2)

[15]

[TURN OVER]

QUESTION 3 (15 marks)

A two variable regression has the following results

Source of variation	Sum of squares (SS)	Degrees of freedom (d.f.)	MSS = SS/d.f.
Due to regression (ESS)	66965	–	–
Due to residual (RSS)	–	–	–
Total (TSS)	67052	29	–

(a) What is the sample size (N)? (2)

(b) What is the value of RSS? (2)

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[15]

SUBTOTAL SECTION A [60]

[TURN OVER]

[TURN OVER]

QUESTION B3 (20 marks)

A regression has been run to estimate the average hourly wages of full time workers. For the purpose of this let

AHE = average hourly earnings (constant 1998=100)

University = binary variable (1 if in university, 0 if in high school)

Female = binary variable (1 if female, 0 if male)

Age = age in years

North, East, South = binary variables (1 if in region, 0 otherwise)

$$\text{AHE} = 3.75 + 5.44 (\text{University}) - 2.62 (\text{Female}) + 0.29 (\text{Age}) + 0.69 (\text{North}) + 0.60 (\text{East}) - 0.27 (\text{South})$$

Other statistics $R^2 = 0.194$, $n = 4000$

- (a) Do there appear to be important regional differences (3)

- (b) Why is the explanatory variable for region = West, omitted from the regression? What would happen if it was included? (3)

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Appendix 1: Formulae sheet

<p>OLS estimates of $Y_i = \beta_0 + \beta_1 X_{1i} + \varepsilon_i$</p> $\hat{\beta}_1 = \frac{\sum x_{1i} y_i}{\sum x_{1i}^2} \text{ where } \begin{cases} x_{1i} = X_{1i} - \bar{X}_1 \\ y_i = Y_i - \bar{Y} \end{cases} \text{ and } i=1 \text{ to } n$ $SE(\hat{\beta}_1) = \sqrt{\frac{\left(\sum e_i^2\right)}{n-2}}{\sum x_{1i}^2}$ <p>$\hat{\beta}_0 = \bar{Y} - \hat{\beta}_1 \bar{X}_1$ where $\bar{Y} = \sum_i Y_i / n$ and $\bar{X}_1 = \sum_i X_{1i} / n$</p>	
<p>TSS (Total sum of squares) = ESS (explained) + RSS (residual)</p> $\sum y_i^2 = \sum (\hat{Y}_i - \bar{Y})^2 + \sum e_i^2$	
<p>OLS estimates of $Y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + \varepsilon_i$</p> $\hat{\beta}_1 = \frac{(\sum y_i x_{1i})(\sum x_{2i}^2) - (\sum y_i x_{2i})(\sum x_{1i} x_{2i})}{(\sum x_{1i}^2)(\sum x_{2i}^2) - (\sum x_{1i} x_{2i})^2} \text{ where } x_{2i} = X_{2i} - \bar{X}_2$ $\hat{\beta}_0 = \bar{Y} - \hat{\beta}_1 \bar{X}_1 - \hat{\beta}_2 \bar{X}_2$ $SE(\hat{\beta}_1) = \sqrt{\frac{\sum e_i^2 / (n-3)}{(\sum x_{1i}^2)(1 - r_{X_1, X_2}^2)}}$	
$r_{X_1, X_2} = \frac{\sum (X_{1i} - \bar{X}_1)(X_{2i} - \bar{X}_2)}{\sqrt{\sum (X_{1i} - \bar{X}_1)^2 \sum (X_{2i} - \bar{X}_2)^2}}$	
<p>Some statistical measures</p> $t = \frac{\hat{\beta} - \beta_{H_0}}{SE(\hat{\beta})}$ $DW d = \frac{\sum_{i=2}^T (e_i - e_{i-1})^2}{\sum_{i=1}^T e_i^2}$ $F = \frac{ESS / K}{RSS / (n - K - 1)}$	

[TURN OVER]

Table	Contents
1	Critical values of the t-distribution
2	Critical values of the F-distribution 5% level of significance
3	Critical values of the Durbin-Watson test statistic (DW-d) of D_L and D_U DW-d 5% one-sided and 10% two-sided level of significance

Table 1 Critical values of the t-distribution

Degrees of freedom	Level of significance					
	One-sided Two-sided	10% 20%	5% 10%	2.5% 5%	1% 2%	0.5% 1%
1		3.078	6.314	12.706	31.821	63.657
2		1.886	2.920	4.303	6.965	9.925
3		1.638	2.353	3.182	4.541	5.841
4		1.533	2.132	2.776	3.747	4.604
5		1.476	2.015	2.571	3.365	4.032
6		1.440	1.943	2.447	3.143	3.707
7		1.415	1.895	2.365	2.998	3.499
8		1.397	1.860	2.306	2.896	3.355
9		1.383	1.833	2.262	2.821	3.250
10		1.372	1.812	2.228	2.764	3.169
11		1.363	1.796	2.201	2.718	3.106
12		1.356	1.782	2.179	2.681	3.055
13		1.350	1.771	2.160	2.650	3.012
14		1.345	1.761	2.145	2.624	2.977
15		1.341	1.753	2.131	2.602	2.947
16		1.337	1.746	2.120	2.583	2.921
17		1.333	1.740	2.110	2.567	2.898
18		1.330	1.734	2.101	2.552	2.878
19		1.328	1.729	2.093	2.539	2.861
20		1.325	1.725	2.086	2.528	2.845
21		1.323	1.721	2.080	2.518	2.831
22		1.321	1.717	2.074	2.508	2.819
23		1.319	1.714	2.069	2.500	2.807
24		1.318	1.711	2.064	2.492	2.797
25		1.316	1.708	2.060	2.485	2.787
26		1.315	1.706	2.056	2.479	2.779
27		1.314	1.703	2.052	2.473	2.771
28		1.313	1.701	2.048	2.467	2.763
29		1.311	1.699	2.045	2.462	2.756
30		1.310	1.697	2.042	2.457	2.750
40		1.303	1.684	2.021	2.423	2.704
50		1.299	1.676	2.009	2.403	2.678
60		1.296	1.671	2.000	2.390	2.660
70		1.294	1.667	1.994	2.381	2.648
120		1.289	1.658	1.980	2.358	2.617
Normal		1.282	1.645	1.960	2.326	2.576

[TURN OVER]

Table 2: Critical values of the F-distribution 5% level of significance

		Degrees of freedom for numerator (v_1)											
		1	2	3	4	5	6	7	8	10	12	20	∞
Degrees of freedom of denominator (v_2)	1	161.0	200.0	216.0	225.0	230.0	234.0	237.0	239.0	242.0	244.0	248.0	254.3
	2	18.5	19.0	19.2	19.2	19.3	19.3	19.4	19.4	19.4	19.4	19.4	19.5
	3	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.79	8.74	8.66	8.53
	4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	5.96	5.91	5.80	5.63
	5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.74	4.68	4.56	4.36
	6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.06	4.00	3.87	3.67
	7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.64	3.57	3.44	3.23
	8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.35	3.28	3.15	2.93
	9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.14	3.07	2.94	2.71
	10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	2.98	2.91	2.77	2.54
	11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.85	2.79	2.65	2.40
	12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.75	2.69	2.54	2.30
	13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.67	2.60	2.46	2.21
	14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.60	2.53	2.39	2.13
	15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.54	2.48	2.33	2.07
	16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.49	2.42	2.28	2.01
	17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.45	2.38	2.23	1.96
	18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.41	2.34	2.19	1.92
	19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.38	2.31	2.16	1.88
	20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.35	2.28	2.12	1.84
	21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.32	2.25	2.10	1.81
	22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.30	2.23	2.07	1.78
	23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.27	2.20	2.05	1.76
	24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.25	2.18	2.03	1.73
	25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.24	2.16	2.01	1.71
	26	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.22	2.15	1.99	1.69
	27	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.20	2.13	1.97	1.68
	28	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.19	2.12	1.96	1.66
	29	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.18	2.10	1.94	1.64
	30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.16	2.09	1.93	1.62
40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.08	2.00	1.84	1.51	
50	4.03	3.18	2.79	2.56	2.40	2.29	2.20	2.13	2.03	1.95	1.78	1.44	
60	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	1.99	1.92	1.75	1.39	
70	3.98	3.13	2.74	2.50	2.35	2.23	2.14	2.07	1.97	1.89	1.72	1.36	
120	3.92	3.07	2.68	2.45	2.29	2.18	2.09	2.02	1.91	1.83	1.66	1.25	
∞	3.84	3.00	2.60	2.37	2.21	2.10	2.01	1.94	1.83	1.75	1.57	1.00	

[TURN OVER]

**Table 3 Critical values of the Durbin-Watson test statistics D_L and D_U
5% one-sided and 10% two-sided level of significance**

n	k'=1		k'=2		k'=3		k'=4		k'=5		k'=6		k'=7	
	d_L	d_U	d_L	d_U	d_L	d_U	d_L	d_U	d_L	d_U	d_L	d_U	d_L	d_U
15	1.08	1.36	0.95	1.54	0.81	1.75	0.69	1.97	0.56	2.21	0.45	2.47	0.34	2.73
16	1.11	1.37	0.98	1.54	0.86	1.73	0.73	1.93	0.62	2.15	0.50	2.39	0.40	2.62
17	1.13	1.38	1.02	1.54	0.90	1.71	0.78	1.90	0.66	2.10	0.55	2.32	0.45	2.54
18	1.16	1.39	1.05	1.53	0.93	1.69	0.82	1.87	0.71	2.06	0.60	2.26	0.50	2.46
19	1.18	1.40	1.07	1.53	0.97	1.68	0.86	1.85	0.75	2.02	0.65	2.21	0.55	2.40
20	1.20	1.41	1.10	1.54	1.00	1.68	0.89	1.83	0.79	1.99	0.69	2.16	0.60	2.34
21	1.22	1.42	1.13	1.54	1.03	1.67	0.98	1.81	0.83	1.96	0.73	2.12	0.64	2.29
22	1.24	1.43	1.15	1.54	1.05	1.66	0.96	1.80	0.86	1.94	0.77	2.09	0.68	2.25
23	1.26	1.44	1.17	1.54	1.08	1.66	0.99	1.79	0.90	1.92	0.80	2.06	0.72	2.21
24	1.27	1.45	1.19	1.55	1.10	1.66	1.01	1.78	0.93	1.90	0.84	2.04	0.75	2.17
25	1.29	1.45	1.21	1.55	1.12	1.66	1.04	1.77	0.95	1.89	0.87	2.01	0.78	2.14
26	1.30	1.46	1.22	1.55	1.14	1.65	1.06	1.76	0.98	1.88	0.90	1.99	0.82	2.12
27	1.32	1.47	1.24	1.56	1.16	1.65	1.08	1.76	1.00	1.86	0.93	1.97	0.85	2.09
28	1.33	1.48	1.26	1.56	1.18	1.65	1.10	1.75	1.03	1.85	0.95	1.96	0.87	2.07
29	1.34	1.48	1.27	1.56	1.20	1.65	1.12	1.74	1.05	1.84	0.98	1.94	0.90	2.05
30	1.35	1.49	1.28	1.57	1.21	1.65	1.14	1.74	1.07	1.83	1.00	1.93	0.93	2.03
31	1.36	1.50	1.30	1.57	1.23	1.65	1.16	1.74	1.09	1.83	1.02	1.92	0.95	2.02
32	1.37	1.50	1.31	1.57	1.24	1.65	1.18	1.73	1.11	1.82	1.04	1.91	0.97	2.00
33	1.38	1.51	1.32	1.58	1.26	1.65	1.19	1.73	1.13	1.81	1.06	1.90	0.99	1.99
34	1.39	1.51	1.33	1.58	1.27	1.65	1.21	1.73	1.14	1.81	1.08	1.89	1.02	1.98
35	1.40	1.52	1.34	1.58	1.28	1.65	1.22	1.73	1.16	1.80	1.10	1.88	1.03	1.97
36	1.41	1.52	1.35	1.59	1.30	1.65	1.24	1.73	1.18	1.80	1.11	1.88	1.05	1.96
37	1.42	1.53	1.36	1.59	1.31	1.66	1.25	1.72	1.19	1.80	1.13	1.87	1.07	1.95
38	1.43	1.54	1.37	1.59	1.32	1.66	1.26	1.72	1.20	1.79	1.15	1.86	1.09	1.94
39	1.43	1.54	1.38	1.60	1.33	1.66	1.27	1.72	1.22	1.79	1.16	1.86	1.10	1.93
40	1.44	1.54	1.39	1.60	1.34	1.66	1.29	1.72	1.23	1.79	1.18	1.85	1.12	1.93
45	1.48	1.57	1.43	1.62	1.38	1.67	1.34	1.72	1.29	1.78	1.24	1.84	1.19	1.90
50	1.50	1.59	1.46	1.63	1.42	1.67	1.38	1.72	1.34	1.77	1.29	1.82	1.25	1.88
55	1.53	1.60	1.49	1.64	1.45	1.68	1.41	1.72	1.37	1.77	1.33	1.81	1.29	1.86
60	1.55	1.62	1.51	1.65	1.48	1.69	1.44	1.73	1.41	1.77	1.37	1.81	1.34	1.85
65	1.57	1.63	1.54	1.66	1.50	1.70	1.47	1.73	1.44	1.77	1.40	1.81	1.37	1.84
70	1.58	1.64	1.55	1.67	1.53	1.70	1.49	1.74	1.46	1.77	1.43	1.80	1.40	1.84
75	1.60	1.65	1.57	1.68	1.54	1.71	1.52	1.74	1.49	1.77	1.46	1.80	1.43	1.83
80	1.61	1.66	1.59	1.69	1.56	1.72	1.53	1.74	1.51	1.77	1.48	1.80	1.45	1.83
85	1.62	1.67	1.60	1.70	1.58	1.72	1.55	1.75	1.53	1.77	1.50	1.80	1.47	1.83
90	1.63	1.68	1.61	1.70	1.59	1.73	1.57	1.75	1.54	1.78	1.52	1.80	1.49	1.83
95	1.64	1.69	1.62	1.71	1.60	1.73	1.58	1.75	1.56	1.78	1.54	1.80	1.51	1.83
100	1.65	1.69	1.63	1.72	1.61	1.74	1.59	1.76	1.57	1.78	1.55	1.80	1.53	1.83

n=number of observations

k'=number of explanatory variables excluding the constant term

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